Associative learning of scene parameters from images

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An important problem for both biological and machine vision is the construction of scene representations from 2-D image data that are useful for recognition. One problem is that there can be more than one world out there giving rise to the image data at hand. Additional constraints regarding the nature of the environment have to be used to narrow the range of solutions. Although effort has gone into understanding these constraints, relatively little has been done to understand how neural-like learning networks may be used to solve scene-from-image problems. A paradigm is proposed in which stochastic models of scene properties are used to provide samples of image and scene representations. Distributed associative networks are taught, by example, the statistical constraints relating the image to the representation of the scene. This technique is applied to problems in optic flow, shape-from-shading, and stereo.

I. Introduction

Recent research has demonstrated the potential of massively parallel architectures for cognitive science. The need for parallel architectures is especially apparent in perception, and in particular vision. To begin to understand the role of neurons and their connectivity in vision, it is necessary to determine what they compute and how they do it. One major problem in vision is the estimation of scene properties from image data.

The image is a description of the luminance as a function of space and time. The scene is a description of objects, their space–time relations, and the illumination and viewing conditions that caused the image. One step in solving the problem of visual recognition in natural conditions has been to construct explicit scene representations from image data. This is because recognition can then be based on representations which are less sensitive to lighting conditions, viewpoint of the observer, and position and orientation of the object. One intermediate goal has been to construct a unified representation of object surface information such as orientation, depth, and reflectance, inferred from various sources of information such as stereo, motion, and color. These representations, or "intrinsic images," differ from more abstract representations by being spatially indexed and in a viewer-centered coordinate frame. However, the computation of scene representations has proved unexpectedly difficult. One reason for the difficulty is that these problems are often underconstrained or ill-posed. That is, there are many possible states of the world which could give rise to a given image.

II. Theoretical Background

A. General

The inference problem of finding the scene which caused an image can be formalized statistically as follows. Let a family of scene parameters be represented by a vector \( s \). The forward problem of calculating an image \( i \) from \( s \) is usually straightforward:

\[
i = A(s),
\]

where \( A \) may, in general, be a nonlinear mapping. However, the inverse problem, of computing \( s \) from \( i \) with a knowledge of \( A \), is ill-posed in the sense that there often is not a unique \( s \) which satisfies the equation.

One approach to solving the inverse problem is maximum a posteriori (MAP) estimation. Suppose the probability of \( s \) conditional on \( i \) is known. The computational goal is then to compute the most probable scene vector, conditional on the image vector. It is often difficult to write directly an expression for the conditional probability. However, Bayes rule enables us to break the probability into two parts:

\[
p(s|i) = \frac{p(i|s)p(s)}{p(i)},
\]

where \( p(i|s) \) and \( p(s) \) characterize the image formation and scene models, respectively; \( p(i) \) is constant. If we assume

\[
i = As + \text{noise},
\]

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Received 15 May 1987.
0003-6935/87/234999-08$02.00/0.
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where the noise term is multivariate Gaussian with a constant diagonal covariance matrix, then
\[ p(\mathbf{i}s) = k \exp \left( -\frac{1}{2\sigma^2} (\mathbf{i} - \mathbf{A}s)^T(\mathbf{i} - \mathbf{A}s) \right), \]  \hspace{1cm} (4)

where \( k \) is a constant. Further, assume that \( p(s) \) is multivariate Gaussian:
\[ p(s) = k \exp \left( -\frac{1}{2\sigma^2} \mathbf{s}^T\mathbf{B}\mathbf{s} \right), \]  \hspace{1cm} (5)

where \( \mathbf{s} \) is adjusted to have zero mean. With these assumptions, and by taking the logarithm of the expression for \( p(\mathbf{i}s) \), maximizing \( p(\mathbf{i}s) \) is equivalent to minimizing
\[ (\mathbf{A}s - \mathbf{i})^T(\mathbf{A}s - \mathbf{i}) + \lambda\|\mathbf{s}\|^2, \]  \hspace{1cm} (6)

where \( \lambda \) is a Lagrange multiplier equal to the ratio of the noise-to-scene variance.

Given a vector representation and the above Gaussian assumptions, the MAP formulation is equivalent to the regularization theory formulation of Poggio et al.\textsuperscript{10} In the regularization approach, one typically incorporates a suitable constraint operator, \( \mathbf{P} \), which reflects our prior assumptions about what \( s \) is usually like (e.g., natural surfaces are smooth almost everywhere). The solution is found by minimizing
\[ \|\mathbf{A}s - \mathbf{i}\|^2 + \lambda\|\mathbf{ps}\|^2, \]  \hspace{1cm} (7)

where the norm may be the squared vector length. Thus, the MAP formulation (6) gives the cost function (7) when \( \mathbf{B} = \mathbf{P}^T\mathbf{P} \). The form of \( \mathbf{P} \) is usually arrived at by a combination of heuristics, mathematical convenience, and experiment.

Expressing regularization theory in terms of MAP estimation has the following advantages. First, it provides a more general framework within which to compare diverse biological and machine implementations that attempt to solve the same problem. Second, the constraint term can, in principle, be based on verifiable scene statistics rather than heuristics. Finding a good statistical model of natural scene parameters is a difficult problem in itself. Here we may benefit from the rapidly expanding field of computer synthesis of naturalistic scenes. Third, the probabilistic formulation defines the input/output pairs to use associative connectionist algorithms that learn to estimate scene parameters from images. This becomes particularly interesting when it is difficult to compute the posterior distribution, and we have a complete description of the prior distribution and the image formation model. Here, of course, we may not be able to directly address the optimality of the learning algorithm, but we can compare its asymptotic performance for scene estimation with human observers. Thus, connectionist learning algorithms can be used as tools to find mappings from image data to scene parameters.

When the image formation process is linear and the prior distribution Gaussian, the cost function is convex, and thus standard techniques, such as gradient descent, can be used to find the global minimum. It seems reasonable to first study linear algorithms for those scene-from-image problems where the computational power is adequate. Quasilinear systems are not uncommon in early visual coding.\textsuperscript{14-16} In the studies below, we show applications of line estimators to problems in optic flow measurement, shape-from-shading, and stereo, away from discontinuities. The MAP formulation can be extended to discontinuities and thus, nonconvex cost functions.\textsuperscript{13} Recent work has demonstrated the potential of analog neural networks to solve these.\textsuperscript{17}

B. Learning Scene Representations from Images

Suppose we have examples of input/output pairs \((\mathbf{i}, s)\), but \( \mathbf{A} \) and \( \mathbf{B} \) are unknown. Then the inverse operator can be estimated using associative learning. This approach can be contrasted with the usual procedure of trying to guess a suitable constraint operator \( \mathbf{B} \). If \( \mathbf{S} \) is the matrix mapping \( \mathbf{i} \) to \( \mathbf{s} \), then \( \mathbf{S} \) can be estimated by the well-known Widrow-Hoff error correction procedure iteratively as follows:
\[ \mathbf{S}_{k+1} = \mathbf{S}_k + \rho_k(\mathbf{s}_k - \mathbf{i}_k)\mathbf{i}_k^T, \]  \hspace{1cm} (8)

where \( \mathbf{S}_k \) and \( \mathbf{i}_k \) are the \( k \)th examples of the surface and image vector representations, respectively; \( \rho_k \) is a scalar often chosen proportional to \( 1/k \) to obtain convergence.\textsuperscript{18-20}

In the three sections which follow, we apply linear associative learning to three different problems in early vision. In addition, each is approached from a slightly different view. The motion measurement problem is a good example of a linear generalized inverse problem.\textsuperscript{21} However, simple rigid motion in the plane is typically over constrained rather than underconstrained. There are data on the neurons which may be subserving measurement of rigid motions in the plane. The problem is that a single neuron may simultaneously carry information about direction and speed. Widrow-Hoff learning is used to find a map between component and pattern-selective model neurons.

Both shape from shading and stereo are examples of nonlinear problems in early vision. Further, shape from shading, in particular, is severely underconstrained. However, by narrowing the domain of the problem, we show both successes and limitations of the linear techniques.

III. Motion Measurement

The aperture problem involves assigning a unique velocity to an object given by local motion measurements. Local motion measurements along contours of the object provide ambiguous information about the direction of motion because only the component of motion perpendicular to the orientation of the moving contour can be measured (Fig. 1).

We implemented this constraint in a model\textsuperscript{22} structured in accord with the following neurophysiological findings.\textsuperscript{23} Some neurons in striate cortex (area V1) are selective for orientation and speed at a given spatial frequency. However, they only respond to the perpendicular component of motion. Area MT, an
with speed $q$. Here, $r_{ij}$ and $R_{pq}$ play the roles of image (i) and scene (s) representations, respectively. Because direction and speed information are multiplexed at the input and output, it is not straightforward to determine the appropriate synaptic weights connecting the model V1 neurons to MT. The linear associator with Widrow-Hoff error correction was employed as a tool to find the weightings represented by matrix $W$ appropriate for a training set consisting of pairs of vectors $(r, R)$, where the elements of $r$ and $R$ are $r_{ij}$ and $R_{pq}$.

One simulation will be described to illustrate the performance of the system. For this simulation, direction-selective units were placed at 15° intervals with bandwidths of 90°. The response tapered off linearly to 0 at 45° on both sides of the peak direction. There were seventeen peak directions (spanning 255°) and eight peak speeds (spanning 30° of visual angle/s). Since each unit is sensitive to both speed and direction, a total of 136 units was available at each location. There were two complete sets (i.e., two locations) of V1 units and one set of MT units. The system was trained on fifty patterns and then tested on these patterns and on fifty new ones (Fig. 2). After fifteen iterations through the training set (with a constant $p_0$ of 0.95), the system reached stable performance and was tested. The mean cosine between estimated and actual pattern velocity was 0.98 and 0.97 for old and novel pattern motion vectors, respectively. Because of the receptive field overlap, the motion information is actually distributed over the population of model MT neurons. A weighted average of MT neurons was taken as a measure of estimated pattern direction and speed:

\[
\text{pattern direction} = \frac{\Sigma R_{pq}p}{\Sigma R_{pq}},
\]

\[
\text{pattern speed} = \frac{\Sigma R_{pq}q}{\Sigma R_{pq}}.
\]

The mean difference between the weighted average for the real direction and the reconstructed direction for the old patterns was 3.0°, while the mean difference for the new patterns was 4.2°. The mean difference between weighted averages for real and reconstructed speeds for old patterns was 1.1°/s compared to 1.6°/s for new patterns.

The model works well for rigid planar motion. Fu-

![Fig. 1. Solution to the ambiguity of motion resulting from local motion measurements for rigid motion in the plane.](image)

extrastriate area involved in motion analysis, receives a direct topographic projection from V1, is selective for the direction and speed of motion of a stimulus, and possesses larger receptive fields, indicating spatial summation of its inputs. Moreover, ~25% of MT neurons exhibit pattern direction selectivity. That is, in contrast to V1 cells, they are selective for the motion of the pattern as a whole, rather than to just a component of the motion.

A network was simulated which mapped activities of component selective V1 neurons to pattern selective MT output units. The activities of the neurons were a result of an instantaneous change in the velocity of a pattern. These model neurons were tuned to particular speeds and directions. Model V1 units signaled only the component of motion perpendicular to their preferred orientation; model MT units responded to 2-D motion.

Let $d_{kl}$ and $s_{kl}$ represent direction and speed of a contour (perpendicular to the orientation) at location $(k,l)$. Then the response of a model V1 neuron with preferred direction $i$ and speed $j$ is

\[ r_{ij} = w_i(d_{kl}) + w_j(s_{kl}). \]  (9)

If we assume identical tuning functions $w(\cdot)$ which are just shifted versions of each other, this expression can be simplified to

\[ r_{ij} = w_d(d_{kl} - i) + w_s(s_{kl} - j). \]  (10)

We seek a linear mapping $W$,

\[ W: [r_{ij}] \rightarrow [R_{pq}], \]

where $R_{pq}$ is the response of a model MT neuron selective for pattern motion in preferred direction $p$ and

![Fig. 2. Examples of patterns used to train the linear pattern velocity estimator.](image)
ture work will determine if the model can be extended to deal with general 3-D motion. Extensions to multiple moving objects will necessarily involve processing of discontinuities in the flow field.

IV. Shape from Shading

The shading pattern on a surface provides information about the shape of the surface. Recent studies of human perception of shape from shading focus on simple convex objects with occluding boundaries, the most common being ellipsoids and spheres. Without the information provided by the boundaries, these images appear very flat. On the other hand, shaded images of more complex surfaces, with several peaks and valleys, are perceived as having 3-D shape. The goal of this research is to investigate the means by which the shape of complex surfaces may be derived solely from shading information, in the absence of occluding boundaries.

Shading is defined as the pattern of luminance reflected from a surface to the viewer. Ignoring the effects of shadows, the luminance at each point of a surface is a function of the surface's albedo, its local geometry (or shape), the position of the viewer relative to the surface, and the lighting conditions. This may be summarized as

\[ L(x,y) = [R(x,y), N(x,y), V(x,y), E(x,y)], \] (13)

where L is the luminance, R is the albedo, N is a representation of the shape of the surface, V is the viewer angle and E is the vector pointing towards the light source with magnitude equal to the light energy flux incident on the surface. The human visual system is thus presented with the formidable task of tearing apart the relative effects of several different variables on the shading pattern.

A first step in simplifying the luminance function is to split it into two independent components, the albedo function R, and the effective illumination I:

\[ L(x,y) = R(x,y)[N(x,y), V(x,y), E(x,y)]; \] (14)

I is then the shading pattern over the same surface with constant albedo. We will ignore the problem of determining R, which, in principle, may be derived independently of the surface shape. Previous modeling work on shape from shading has relied on several assumptions which further simplify Eq. (13). These are that the surface is Lambertian (i.e., luminance at a point is constant for all viewing directions), and the light source is a point source at infinity with known direction. The first of these remains to be adequately tested. The second may be defended by noting that many complex lighting conditions may be modeled fairly well by a point light source and that the direction of the source may be accurately determined from image statistics.\(^{(26)}\) Equation (13) now reduces to

\[ L(x,y) = kN(x,y) \cdot E, \] (15)
a constant times the dot product between the surface normal vector and the normal vector E in the direction of the light source. The only unknown left to solve for is the set of surface normals, \([N(x,y)].\)

A. Surface Model

One must somehow constrain the space of possible surfaces. Previous research has focused on the use of constraints on the local structure of surfaces, such as a smoothness constraint and the umbilical point approximation.\(^{(27,28)}\) The approach taken here is to assume that surfaces are constrained by their global statistical structure and to apply an associative learning algorithm to learn a shape-from-shading operator which embodies those constraints. Theoretically, the form of the constraints need not be known a priori, if a test set of natural surfaces exists on which the model may be trained.

As it would be difficult to obtain enough examples of real surfaces to adequately span the surface space, we generate the surfaces on which the model will be trained using a statistical fractal model.\(^{(29)}\) Random fractal functions are characterized by their statistical self-similarity, expressed in the following relationship:

\[ p \left[ \frac{F(x + \Delta x) - F(x)}{|\Delta x|^H} < \gamma \right] = F(\gamma). \] (16)

F, the random fractal function, and x may be vector-valued. The fractal dimension, D, of the function F is

\[ D = E + 1 - H, \] (17)

where E is the topological dimension of the function. This relation expresses the invariance of the statistics of S over changes of scale. For a fractal surface, the fractal dimension is somewhere between 2 and 3, the fractional part, in some sense, specifying how much of 3-D space the surface is filling. The fractal dimension may be related to the power spectrum of F by

\[ S(f) = 1/f^b, \quad b = 3 - 2(D - E). \] (18)

For spatially isotropic surfaces, f corresponds to radial spatial frequency, so the power spectrum (and thus, the autocorrelation function) is circularly symmetric. This last relation provides the means by which we generate random pseudofractal surfaces. We filter Gaussian white noise through a filter with the appropriate power spectrum to generate a lattice of surface depths. The parameters needed to specify such a surface are the fractal dimension, the cutoff frequencies of the generating filter (if we bandpass the surfaces), and the variance of the surface depths.

B. Linear Estimation of Shape-from-Shading

The ideal shape-from-shading operator will necessarily be nonlinear, due to the nonlinearity in the imaging Eq. (15). It is of interest, however, to study the performance of linear shape-from-shading operators. Such an operator will perform poorly at boundaries and regions of shadow; however, it may otherwise be quite accurate and can be used to derive a first-guess for a nonlinear model which incorporates contour and shadow information.

We used the Widrow-Hoff error-correcting learning rule to derive a shape-from-shading operator from examples of shapes and their images. With the assumption that surfaces are examples of a wide-sense station-
ary process (their statistics are spatially invariant), we can derive a local convolution operator by associating the shape representation at a point on a surface with the image of the surrounding region. The resulting rows of the association matrix will be FIR filters which can be applied to large images to reconstruct surface representations.

Images were represented as vectors of luminance contrast values at each point in the image:

$$I(x,y) = \frac{I(x,y) - \mathbb{E}(L)}{\mathbb{E}(L)},$$  \hspace{1cm} (19)

where $\mathbb{E}[-]$ indicates expected value. A simple statistical analysis of the images of isotropic surfaces will serve to motivate the selection of luminance contrast as the image representation. A principal requirement for the input representation is that it be constant-mean for different settings of the surface generation parameters. If we represent the light source direction vector as $(l_x, l_y, l_z)$ and the surface normal at a point as $(n_x, n_y, n_z)$, for the mean luminance in the image we have

$$\mathbb{E}[L] = \mathbb{E}[k(l_x n_x + l_y n_y + l_z n_z)],$$

$$\mathbb{E}[L] = k \mathbb{E}[E(n_x)] + 1 \mathbb{E}[E(n_y)] + 1 \mathbb{E}[E(n_z)].$$

Due to the isotropic nature of the surfaces, $\mathbb{E}[n_x] = \mathbb{E}[n_y] = 0$, giving

$$\mathbb{E}[L] = k \mathbb{E}[n_z].$$  \hspace{1cm} (20)

As $\mathbb{E}[n_z]$ is a monotonic decreasing function of the variance of surface depths, raw luminance values are clearly an inappropriate input representation. A second requirement for the input representation is that it be invariant to changes in surface albedo and incident light flux (captured in the constant $k$ above). Image contrast, as given by Eq. (19), fulfills both of these requirements, as $k$ cancels out and $\mathbb{E}[I] = 0$ for all spatially isotropic surfaces.

Surfaces were represented as vectors of surface normal components at each point. Thus, we are associating an $n \times n$ image with the three surface normal components at the center point of a surface. The rows of the resulting association matrix may be applied as convolution filters to images to estimate the surface normals at each point in the images. Simulations were also run using surface orientation as the output representation; however, the resulting filters did not perform as well as those for surface normals, and so will not be described here.

We generated a set of 800 29 x 29 pixel surfaces and their corresponding images for fractal surfaces with dimension 2.2. The images were generated using a model light source at a tilt of 45° and a slant (away from the viewer) of 35°. The images were associated with the middle points of their corresponding surfaces to derive the convolution filters. These filters can be used for light source tilts other than 45° by reorienting them relative to the new light source direction. Figure 3 shows the impulse response of the learned filters for the $x$ and $y$ components of the surface normals. Figure 4 shows two test surfaces and the surfaces recon-
stuctured using the learned filters. Note that the first is an artificially generated smooth surface and the second is a low-pass filtered fractal surface. It is particularly interesting to note that the model performed well on a regular surface not generated by the same algorithm as those on which the model was trained. The only significant error in the reconstruction is the smoothing of the discontinuities, as should be expected from a linear operator.

The model makes a significant psychological prediction: the slant bias and low-frequency undulations in the surface will be lost in the reconstruction. The first prediction results from the form of the input vectors. Although the image contrasts for the training phase of the simulations were generated using the statistical mean of the image luminances, those used during testing were computed using the sample mean luminance of the test image. Thus, inputs to the model will always be zero mean. The significance of this is that the reconstructed surface normals will be zero mean. This is intuitively appealing, as changes in mean luminance caused by such a bias can be easily attributed to changes in the surface albedo or in the intensity of the incident light flux. The second prediction, that low-frequency changes in shape will not be reconstructed, is attributable to the bandpass nature of the derived filters. It will be interesting to see if psychophysical studies bear out these predictions.

V. Stereo

The problem of extracting the structure of the environment from stereo cues has traditionally been considered as a two-part problem. The correspondence problem refers to the pairing of points in the left and right eye images that correspond to a single point on the object’s surface. Once these correspondences are known, along with the fixation point, the relative depths of points along the surface may be reconstructed using simple trigonometric relations. Since the introduction of random-dot stereograms and the subsequent popularity of computational approaches to modeling stereo, it has become evident that the correspondence problem is not a trivial one. Nonetheless, the fact that the problem can be solved by low-level visual information is apparent by viewing random-dot stereograms. From a computational point of view, however, it is difficult to specify factors that constrain the problem sufficiently to give a stable surface percept, despite the large number of solutions consistent with the image data.

The approach generally taken in computational models of structure from stereo is to impose physical constraints on the problem to limit the solution space in a way that predicts human perceptual solutions. Marr and Poggio were perhaps the first to explicitly define some of these constraints. They implemented an iterative cooperative algorithm that solves the problem of eliminating false matches using uniqueness, continuity, and compatibility constraints. In addition to these explicit constraints, the model requires the manipulation of a neighborhood size, an inhibition constant, and the threshold value. While Marr and Poggio showed that their model is able to solve a reasonably wide range of random-dot stereograms, different complex combinations of the constraints and associated parameters are optimal for different stimuli.

The approach we have taken has a different focus than previous models in that it attempts to solve the correspondence problem implicitly by directly relating the images on the two retinas to the way the geometry of the environment is changing locally with respect to the fixation point. This scheme emphasizes the importance of the roles of input/output coding on the appropriateness of the algorithm. Thus, while the emphasis in past models has been to eliminate false matches, in this model the pattern of false matches is assumed to be useful for determining the true depth properties of a surface. Thus, in a natural unmarked surface, when the depth is not changing, false matches are found at all disparity cells at that location and at neighboring cells as well, given a primitive such as change in intensity. This assumes that no change in intensity is indeed available as information for the system. When depth does change, there is a corresponding pattern of activity in the cells, again across a variety of spatial locations, that indicates the presence and depth placement of an edge.

We have applied associative learning to the stereo problem to allow appropriate constraints to develop naturally in the system on the basis of the particular set of stimuli presented. The surfaces were generated by a discrete Gaussian Markov process (the probability of depth was conditional on the previous neighbor). However, we make no particular claims about the general validity of such a surface model. No a priori decisions are made about smoothness in the model. Smoothness is defined as a constraint in this model on the basis of the sample images learned. As in the later Marr and Poggio model, this model is aimed at solving a class of surfaces, rather than single surfaces, which require individual adjustments of the model's parameters.

The surfaces were 1-D, Lambertian, and illuminated by a point source at infinity. The surface was viewed along the axis of random depth change, which made occlusion relatively rare. The images are made in an optically natural way that simulates two eyes converged to a fixation point. This adds a regularity to the model in that the disparity at the fixation point, by definition, is always zero. Thus, the issue to be solved is how the disparities change going out from the point of fixation to the periphery. Consistent with this, the resolution of the system decreases in the periphery. The input (image representation) to the model consists of the states of a small number of disparity-sensitive cells that fire to the presence of relatively sharp intensity changes in the left and right eyes at different disparities. The firing rate of these cells is given by

$$ \frac{k}{l_i - r_{i+d} + k} $$

where $l_i$ and $r_i$ are the components of the vector of

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intensity change for the left and right eyes, respectively, $d$ is a disparity offset, and $k$ is a constant. Thus, a perfect match activates the cell to its full firing rate while less perfect matches activate the cell to a lesser degree. An activation function is necessary due to the fact that the surface sample is taken in a natural way by two eyes. As such, the contrast of an edge is not often an exact match when sampled by the left and right eyes, due to the different angle each eye makes with the surface. A small bank of these cells, with both convergent and divergent disparity sensitivities is located at each spatial location in the image. This is meant to emulate the kinds of disparity information the visual system may have to work with.\(^{33}\) For this simple model, input to the model consisted of five disparity cells: two with convergent sensitivities, two with divergent sensitivities, and a zero-disparity cell were used at each spatial position in the retinas. The output of the model was simply the map of surface depth changes.

Connection strengths between the input and output nodes were learned associatively using a Widrow-Hoff error correction technique with 400 surfaces created with the Markov process. The model was tested with thirty new images created in the same manner as the learned images. The cosine between the actual depth map of the tested surface and the depth map produced by the system was used as a performance measure. The average cosine for the thirty vectors tested was 0.765. This indicates good performance, especially given the fact that the images potentially include occluded regions. The form of the inverse mapping is illustrated in Fig. 6. Here we see the average connection strengths that developed in the disparity banks along the diagonal of the matrix. The constructs that developed naturally show a coherent pattern of excitation to same-disparity cells and inhibition in the surrounding disparity cells. These constraints are not unlike those imposed by Marr and Poggio and a variety of other stereo modelers. Some sample images and their reconstructions are shown in Fig. 5. We are currently working on a backpropagation algorithm\(^{6}\) to deal more effectively with the nonlinear nature of the image formation process.

The experiences of many computational stereo modelers over the past two decades have indicated that unique solutions to the ill-posed stereo problem require either that we derive an algorithm that will work for a large number of images if supplied with the proper constraints and parameters, or that we delineate classes of images on which to work. Neither of these approaches is entirely satisfactory. Thus, while modeling approaches are able to work with algorithms that solve the stereo problem given the appropriate constraints, perhaps the most interesting questions are those that tell us what sets of images/surfaces the brain groups together and constrains as a whole.
VI. Conclusion

We have shown that, given models for image and scene representation and an associative algorithm, one can learn to estimate scene parameters from images. Although linear estimators are quite restrictive, they work well when applied away from discontinuities. This paradigm may be particularly useful as more sophisticated statistical scene models are developed. Together with recent developments in nonlinear learning algorithms8 and possible neuronal solutions of non-quadratic cost functions,17 we have potentially powerful tools for exploring early vision.

References


This work was supported by the National Science Foundation under grant BNS-85-18675 and by the Office of Naval Research under contract N-0014-86-K-0600 to J. A. Anderson and BRSG grant PHS2 S07 RR07085.

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